

*Notes for Point-Slope form*

The Point-Slope form for the equation of a straight line is used to write the equation when:

1. The slope of the line and one point on the line is known, or,
2. Two points are known.

Usually a known point is not the  $y$ -intercept. If it were, then the slope-intercept form should be used to write the equation.

**The Point-Slope form of a line:**  $y - y_1 = m(x - x_1)$

where  $m$  is the slope of the line and  $(x_1, y_1)$  is any point that the line passes through

Here are several examples of how to use this form for these situations:

1. How to write an equation **given the slope of a line and a point that the line contains:**

Example: Write the equation of the line that has slope  $-\frac{4}{3}$  and contains point  $(-7, 5)$ .

Answer:  $y - 5 = -\frac{4}{3}(x - (-7)) \rightarrow y - 5 = -\frac{4}{3}(x + 7)$

2. How to write an equation **given two points that lie on the line:**

Example: Write the equation of the line that contains points  $(-4, 6)$  and  $(7, -2)$ .

Answer: First get the slope of the line:  $m = \frac{-2 - 6}{7 - (-4)} = \frac{-8}{7 + 4} = -\frac{8}{11}$

then, use one of the points to write the equation (either one will do). I use the second:

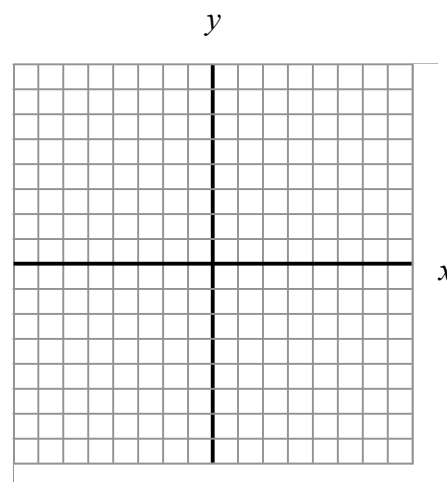
$$y - (-2) = -\frac{8}{11}(x - 7) \rightarrow y + 2 = -\frac{8}{11}(x - 7)$$

3. How to **graph a line in Point-Slope form:**

Example: Graph the line  $y - 4 = -\frac{2}{5}(x + 3)$

Answer: The slope of the line is:  $-\frac{2}{5}$  and the line contains the point  $(-3, 4)$ .

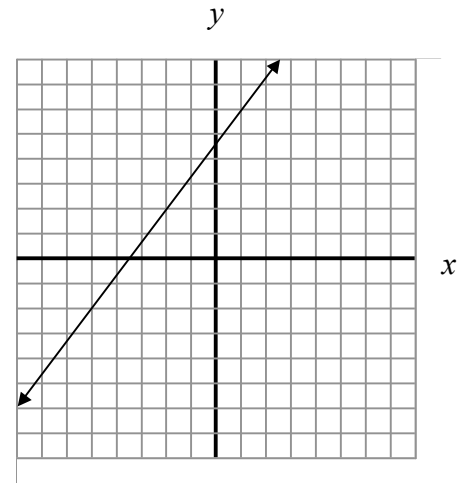
Position the point and then use the slope to show another point and then draw the line.



4. Write an equation of a line that is graphed using Point Slope form when the y-intercept is not known to be an integer.

Example: See graph at right.

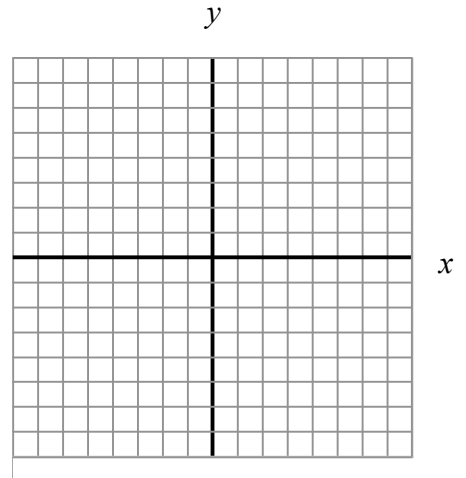
Answer: Identify the slope as  $\frac{4}{3}$  and use one of the known points (1, 6) to get  $y - 6 = \frac{4}{3}(x - 1)$ .



### Practice

**Write an equation** for each line described below using Point-Slope form and **graph each line**.

1. The line with slope  $-\frac{4}{5}$  that contains point (3, -8).



2. The line that contains points (-3, 7) and (-5, -2).

